From Indexing Data Structures to de Bruijn Graphs

Bastien Cazaux, Thierry Lecroq, Eric Rivals

LIRMM & IBC, Montpellier - LITIS Rouen

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Motivation

- De Bruijn Graph is largely used in *de novo* assembly. [Pevzner et al., 2001]
- One builds a suffix tree before the assembly for some applications, for instance for the error correction. [Salmela, 2010]
- There exist algorithms to build directly the De Bruijn Graph. [Onodera et al., 2013] [Rødland, 2013]
- None is able to build the Contracted De Bruijn Graph directly.

Indexing data structures

- Numerous data structures: suffix tree, affix tree, suffix array, etc.
- to index one or several texts (generalized index)
- functionally equivalent to
- compressed versions (CSA, FM-index, CST, etc)

Relation between indexing structures and assembly graphs

- Generalised Suffix Tree (GST)
- indexes all factors of a set of texts
- is functionally equivalent to other indexes (SA, CSA, FM-index)

Relation between indexing structures and assembly graphs

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Question: How to directly build, e.g., the assembly De Bruijn graph? in classical or contracted form?



Generalized Suffix Tree (GST)

2 De Bruijn Graphs



4 Contracted De Bruijn Graph

6 Conclusion and Future works

Generalized Suffix Tree (GST)

Generalized Suffix Tree (GST)

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Generalized Suffix Tree & DBG

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Example

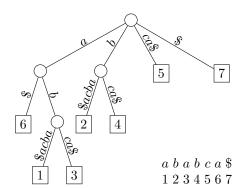
$S = \{bbacbaa, cbaac, bacbab, cbabcaa, bcaacb\}$

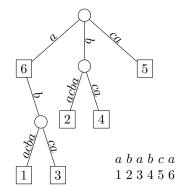
$$||S|| = \sum_{s_i \in S} |s_i|$$

$$||S|| = 7 + 5 + 6 + 7 + 6 = 31$$

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Suffix Tree





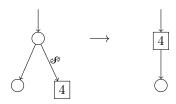
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Feature

take in input a set of words

no use an end marking special symbol
 i.e. no hypothesis requiring that a suffix is not the prefix of another suffix



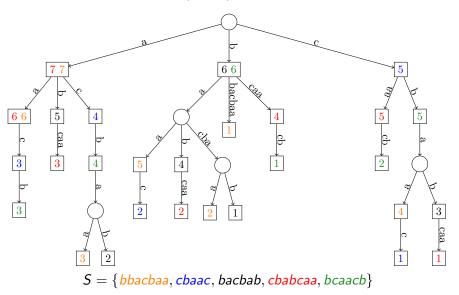
Theorem

The GST of a set of words S takes linear space in ||S||.

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Generalized Suffix Tree (GST)



De Bruijn Graphs

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Generalized Suffix Tree & DBG

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De Bruijn Graph

The assembly De Bruijn Graph (DBG_k^+)

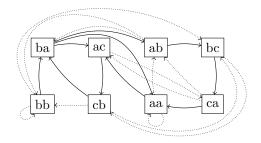
Let k be a positive integer satisfying $k \ge 2$ and $S = \{s_1, \ldots, s_n\}$ be a set of n words. The De Bruijn graph of order k of S, denoted by DBG_k^+ , is a graph such that

- the nodes are the k-mers of S and
- an arc links two k-mers of S if there exists an integer i such that these k-mers start at successive positions in s_i.

Remark: the arc definition implies that the two k-mers overlap by k - 1 positions.

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De Bruijn Graph for assembly



$S = \{bbacbaa, cbaac, bacbab, cbabcaa, bcaacb\}$

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From the Generalized Suffix Tree to the DBG

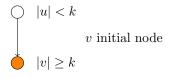
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Generalized Suffix Tree & DBG

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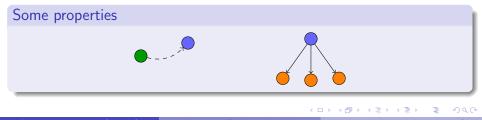
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One defines 3 specific types of nodes in the GST (in V_S):

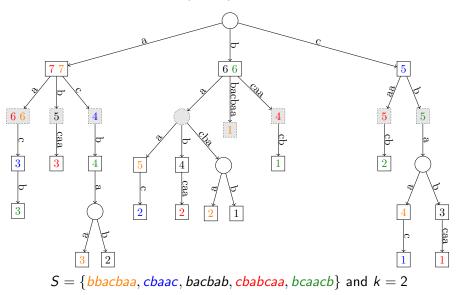


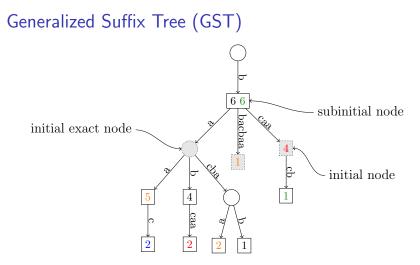
 $|v| = k \quad v \text{ initial exact node}$

$$|v| = k - 1$$
 v subinitial node



Generalized Suffix Tree (GST)





 $S = \{bbacbaa, cbaac, bacbab, cbabcaa, bcaacb\}$ and k = 2

Nodes of the de Bruijn Graph

Notation: Inits

Let $Init_S$ denote the set of initial nodes of the GST of S.

Property: node correspondence

The set of k-mers of DBG_k^+ of S is isomorphic to $Init_S$.

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Arcs of the de Bruijn Graph

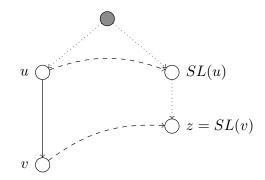
Idea

- Take an initial node v
- I follow its suffix link to node z (lose the first letter of its k-mer)
- \bigcirc if needed, go the children of z to find its extensions
- Output the extensions are valid

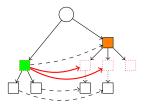
Let v be an initial node, u its father, and z the node pointed at by the suffix link of v.

Property 2

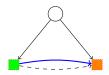
Let v be a node of suffix tree. If it exists, the suffix link of v belongs to the sub-tree of the suffix link of par(v).



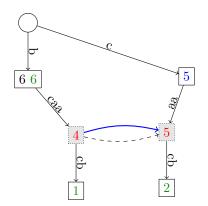
Arcs of DBG_k^+ : case figure



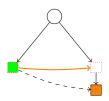
v starting initial node: green z := SL(v) node pointed at by its suffix link: orange black straight arrows : arcs of ST dotted arrows: suffix links colored plain arrows: created arcs of the DBG_{ν}^{+}



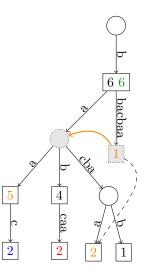
v is initial not exact & *z* is initial



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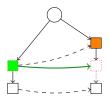


v is initial not exact &
z is not initial
i.e. z is deeper than word
depth k

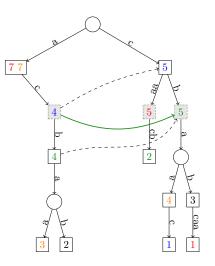


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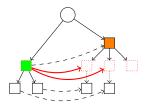
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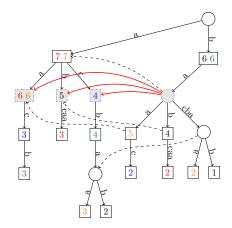
v is initial exact with a single child



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v is initial exact with a several children



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DBG construction

Theorem

Given the GST of a set of words S. The construction of the De Bruijn Graph takes linear time in ||S||.

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DBG construction

Theorem

Given the GST of a set of words S. The construction of the De Bruijn Graph takes linear time in ||S||.

Proof

All four cases of the typology are processed in constant time.

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Contracted De Bruijn Graph

Contracted De Bruijn Graph

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Generalized Suffix Tree & DBG

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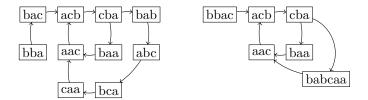
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Image: A match a ma

Example

not contracted

contracted



$S = \{bbacbaa, cbaac, bacbab, cbabcaa, bcaacb\}$

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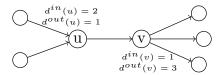
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Left and right extensible nodes

Left or right extensible node

Let v be a node of the De Bruijn graph; we say that

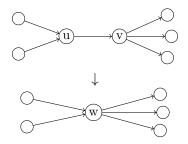
- v is left extensible if and only if $d^{in}(v) = 1$.
- v is right extensible if and only if $d^{out}(v) = 1$.



Contracted De Bruijn Graph

Contracted De Bruijn Graph

Let $G := (V_G, E_G)$ be the De Bruijn graph of order k of S. We call $K := (V_K, E_K)$ the Contracted De Bruijn Graph $(CDBG_k^+)$ of order k of S, the graph obtained from G by contracting iteratively the arcs (u, v) where u is right extensible and v is left extensible.



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Find right extensible nodes

Property 4: right extensible

- Initial nodes of type 1, 2 or 3 are right-extensible.
- Initial nodes of type 4 are not right-extensible.

Find right extensible nodes

Property 4: right extensible

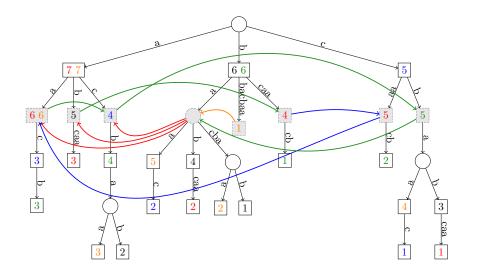
- Initial nodes of type 1, 2 or 3 are right-extensible.
- Initial nodes of type 4 are not right-extensible.

Proof

- Types 1, 2 or 3: word of node v has only one extension in S.
- Types 4 nodes have several extensions in S.

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Case of right extensible nodes ex. for k = 2



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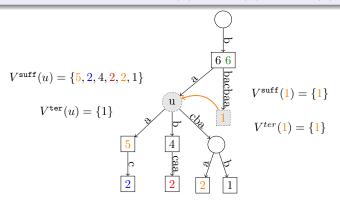
Image: A match a ma

Find left extensible nodes

Let v be a right extensible k-mer/node and (v, u) an arc of DBG_k^+ . Question: is u left extensible?

Property 5: left extensible

u is left extensible if and only if $V^{\text{suff}}(u) - V^{\text{ter}}(u) = V^{\text{suff}}(v)$



Find left extensible nodes

Let v be a right extensible k-mer/node and (v, u) an arc of DBG_k^+ . Question: is u left extensible?

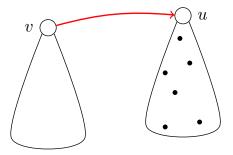
Property 5: left extensible

u is left extensible if and only if $V^{\text{suff}}(u) - V^{\text{ter}}(u) = V^{\text{suff}}(v)$

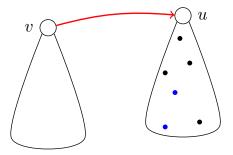
Idea

- determine how many nodes in sub-tree of u have Suffix Links pointing to them coming from the sub-tree of v
- do not account for nodes representing the first suffix of words in S which we call *terminal* nodes
- compare the cardinalities of non terminal suffixes in *u* sub-tree with suffixes in *v* sub-tree.

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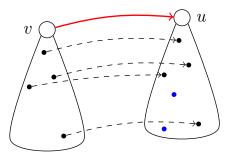


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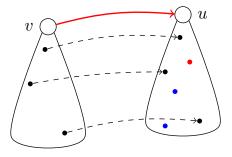
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u is left extensible



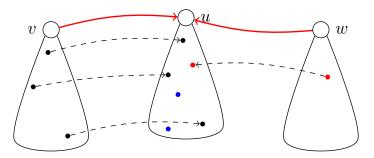
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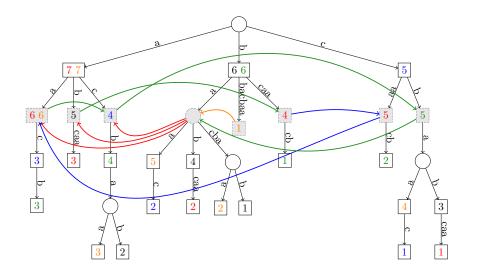
u is **not** left extensible



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Case of left extensible nodes ex. for k = 2



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Contracted DBG construction

Theorem

Given the GST of a set of words S. The construction of the Contracted DBG_k^+ takes linear time in ||S||.

Idea of proof.

Detection of right extensible nodes is obtained from the 4 types.

To get left and right extensible nodes in constant time preprocess:

- $V^{\text{suff}}(u)$ and $V^{\text{ter}}(u)$ for each node u of GST, and
- for each node w of ST such that |w| ≥ k a pointer to its ancestral initial node.

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Conclusion and Future works

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Conclusion

A linear time algorithm that

builds the Contracted De Bruijn Graph

from a Generalized Suffix Tree or a Suffix Array

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Future works

• Use only a slice of the suffix tree

• Update the order of the DBG: dynamically changing k

• Go for compressed indexes instead of a Suffix Tree

Funding and acknowledgments



Thanks for your attention Questions?

Cazaux, Lecroq, Rivals (LIRMM)

Generalized Suffix Tree & DBG

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